

Aeroelastic Analysis CH601XL

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Figure 1: Ground Vibration Test CH601XL



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1. Task description

In this paper, linear aeroelastic investigations on the flutter stability of the aircraft CH601XL are documented in order to show compliance with the requirements of JAR-23. With a complete Ground Vibration Test (GVT) and flutter calculations based on the modal values found in the GVT, linear flutter stability has to be shown up to a true airspeed (TAS) of as much as 120% of the design speed ($1.2 \cdot VD$).

The flutter calculation was initially worked out for the airplane with minimum take-off mass (Empty: No luggage, no fuel, one pilot), free controls and fixed controls at sea level. After this, flutter calculations with maximum take-off weight (pilot and copilot, maximum amount of fuel and maximum luggage), blocked and freed controls at sea level were performed. To show aeroelastic effects of manufacturing tolerances in the ailerons, additional mass points was added to the trailing edge of the ailerons and all previous calculations were repeated. As a last task, the feasibility and desirability of aileron mass balancing was evaluated as a potential modification for the CH601XL. A number of calculations were also made for high-altitude (5,000m) flights for different mass configurations of the CH601XL.

The methods used here to calculate the flutter speed of an aircraft are based on Finite Element Analysis (FEA) and have been verified and validated with several wind tunnel tests³.

The methods used for the evaluation of the time series resulting from the ground vibration tests (GVT) have been verified and validated with both FEA results and experiments⁴.

³ Uwe Weltin, Berechnung und Überprüfung der Flattergeschwindigkeit eines Flügelstreifens im Winkanal des DLR_School_Lab der TUHH, Interne Berichte des Institutes für Zuverlässigkeitstechnik an der TUHH, 2004 .

⁴ Swantje Johnson, Dynamische Strukturanalyse einer Aluminiumplatte, Institut für Zuverlässigkeitstechnik an der Technischen Universität Hamburg, August 2007.

2. Ground Vibration Test

To carry out the vibration tests (GVT), the CH601XL aircraft was equipped with as many as 78 accelerometers (see Figure 2) and suspended from the ceiling of the hangar (see figure 1).

Zodiac CH601XL
 Zenair (09.05.2009)
 (Long range fuel tanks)

- * node(s) reserved for fuel mass: 84, 90, 94, 98, 113, 118, 122, 126
- * node(s) reserved for pilot mass: 147, 148
- * node(s) reserved for baggage mass: 58, 95, 99, 123, 127
- * node(s) reserved for aileron balance (right): 69, 74, 80, 86
- * node(s) reserved for aileron balance (left): 103, 107, 111, 115
- * point masses represent the approximate mass distribution of max. fuel (81.8kg), max. luggage (2x18kg) and max. pilot mass (150kg)
- * all measurement configurations include a cockpit ballast of 75 kg to represent the mass of a single pilot, resulting a suspended weight of 385 kg (natural frequency at 1.60 Hz)
- * max. take-off weight: 450 kg (empty weight+crew+baggage+fuel)
- * empty weight: 310 kg

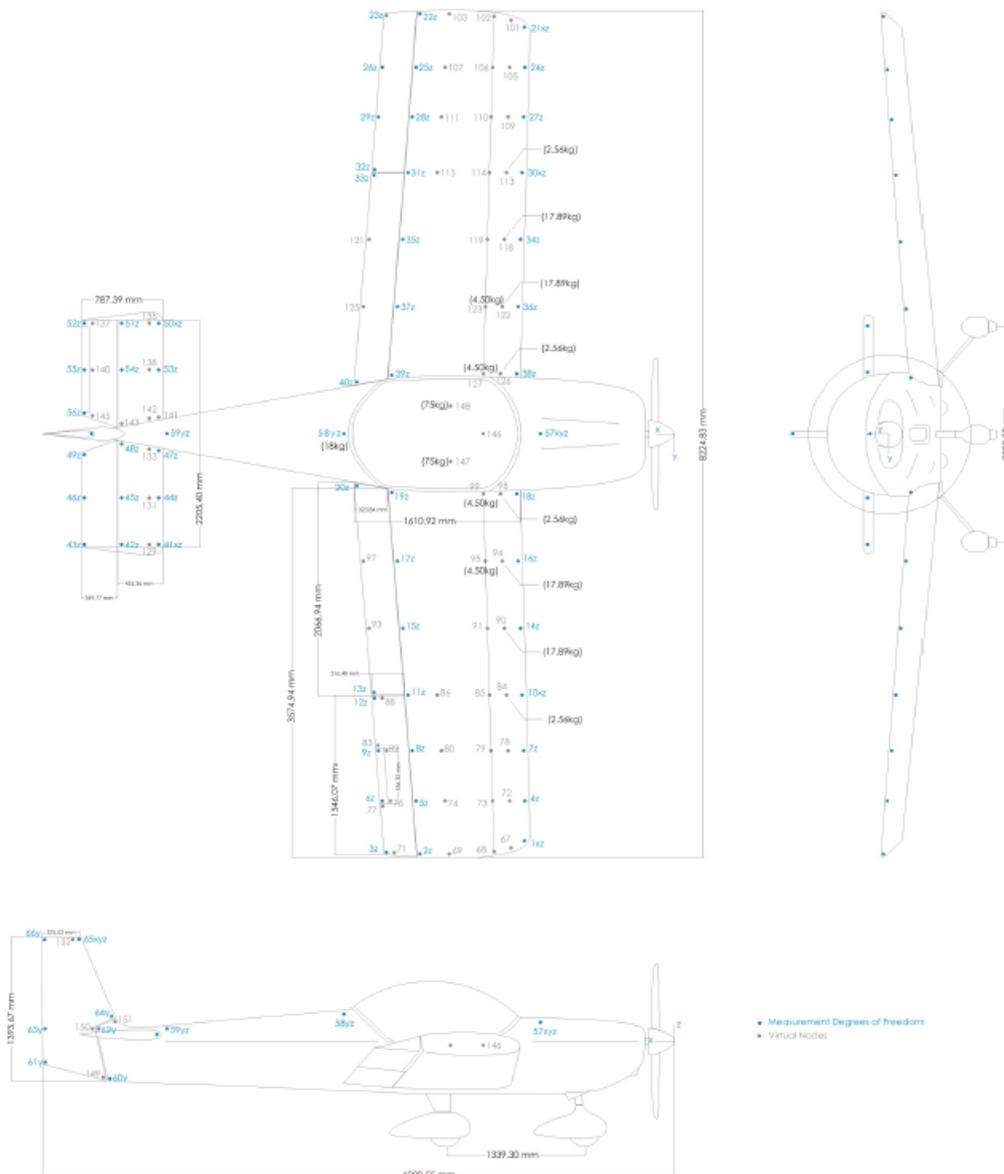


Figure 2: Node numbers for accelerometers and synthetic mass perturbation

The springs of the suspension have an effective stiffness of $C_s = 39 \text{ kN/m}$. The CH601XL in its minimal mass configuration loads 385 kg. The highest rigid body resonance frequency (vertical movement of the total airplane) in its elastic suspension therefore is

- $F_{R1} = 1.6 \text{ Hz}$.

The other rigid body Eigen frequencies of the aircraft are all at considerably lower values. Because the lowest structural mode shapes of the aircraft need to be captured accurately enough, all rigid body natural frequencies have to lie significantly below the first structural Eigen frequency. The first wing bending Eigen frequency is determined at

- $F_{S1} = 10.3 \text{ Hz}$

so that the required frequency spacing is fulfilled. For a complete GVT multiple multi shaker configurations have to be used in order to be able to identify all relevant natural modes. Figure 3 shows the shaker configurations for the identification of the control modes of the CH601XL.

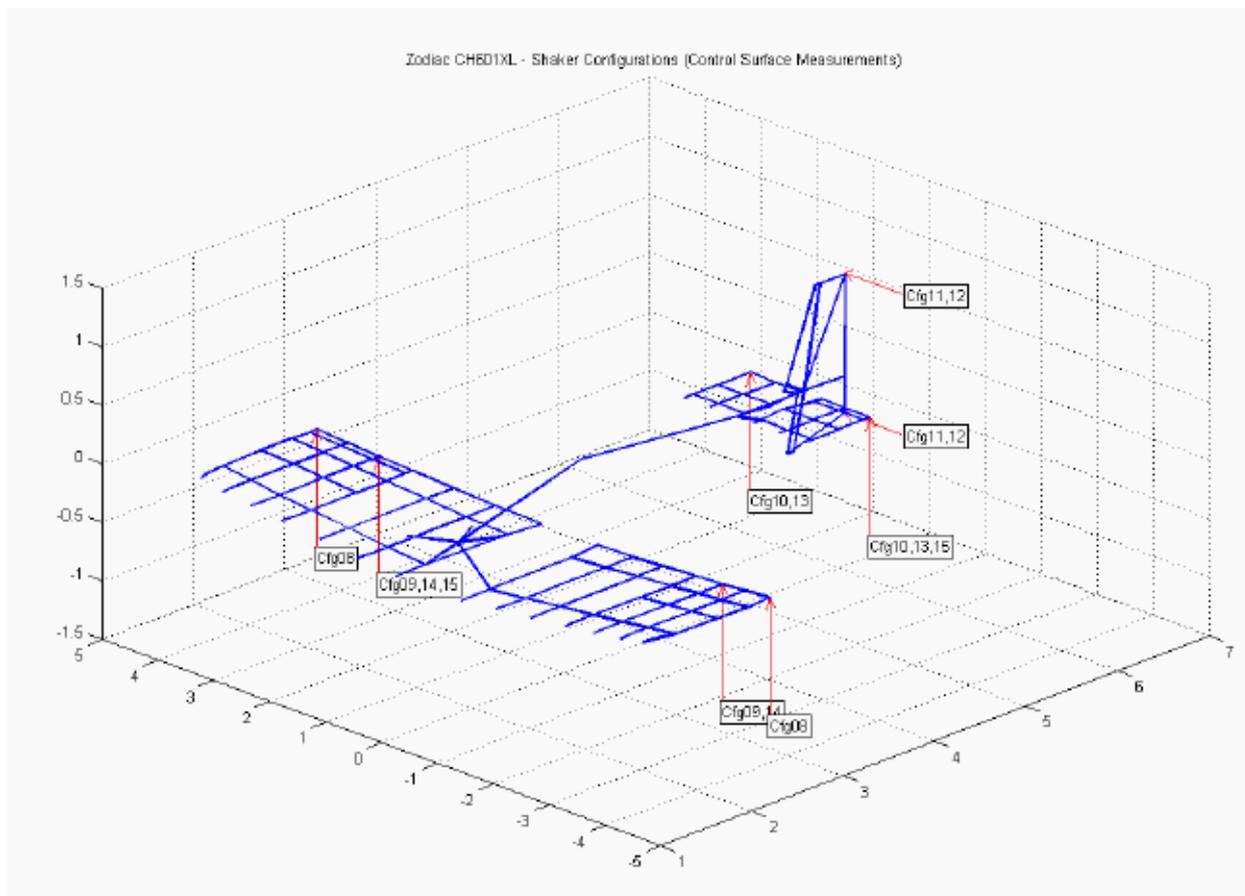


Figure 3: Shaker configurations for the identification of the control modes of the CH601XL

Figure 4 shows the shaker configurations for the identification of the structural modes of the CH601XL.

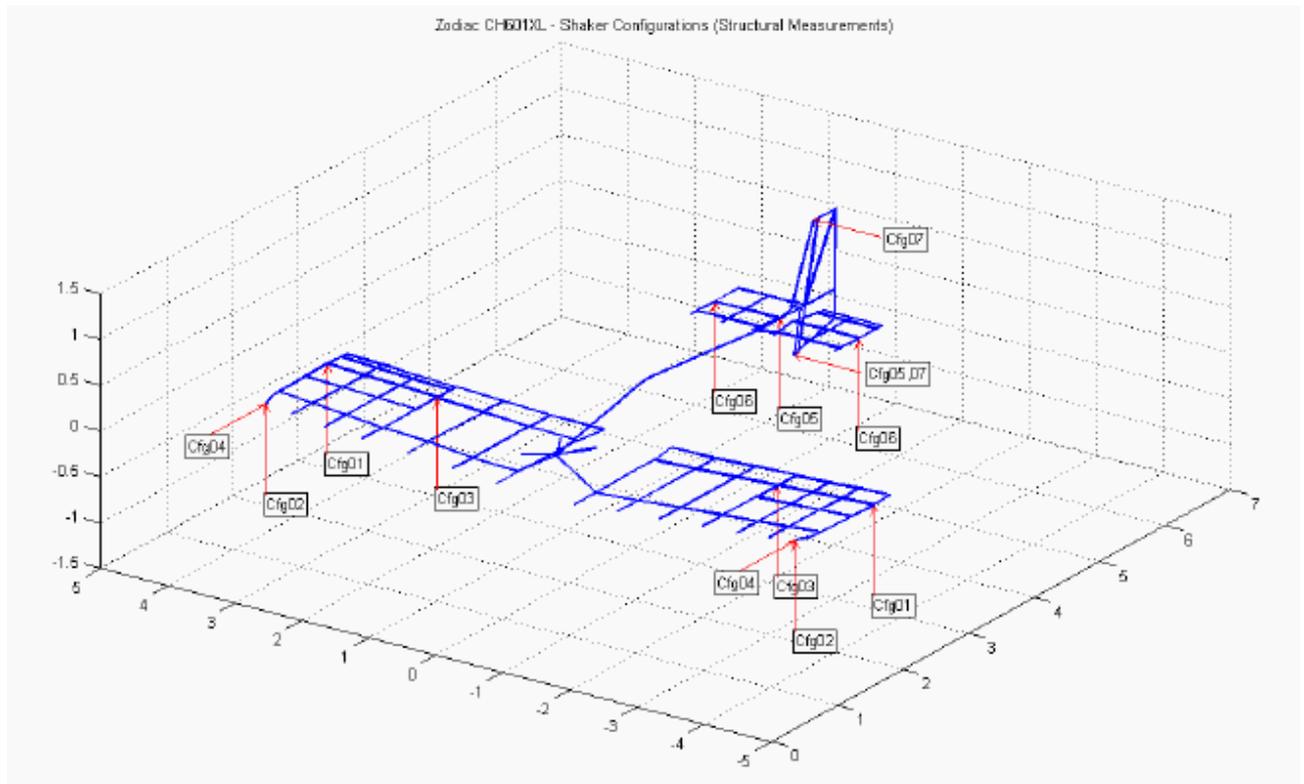


Figure 4: Shaker configurations for the identification of the structural modes of the CH601XL

2.1 Modal data from GVT for CH601XL with minimum take off mass and fixed controls

After evaluating the measurements of the ground vibration test for the CH601XL with minimum take off mass and fixed controls the values for the Eigen frequencies, the generalized masses and modal damping are obtained. The value PRC (Phase Resonance Criterion) is one of the two quality indicators used in this report. If the value PRC is better than 95% the excitation of the corresponding Eigen modes was successful. For PRC values smaller the 80% another measurement with shaker positions in the antinodes of an actual mode is advised.

In order to work out robust flutter margins with respect to the possible variances of control cable tension of the airplane in service, a total of four modal measurements are performed for the CH601XL (see Tables 1 to 3).

A second indication for the quality of the GVT- evaluation is the Modal Assurance Criterion which shows the result of the orthogonality of the Eigen modes found with the ground vibration test (see Figures 5 to7).

Table 1: Modal data from GVT for CH601XL with minimum take off weight and fixed controls, control cables adjusted to 5 lbs

Datafile: CH601XL basic 5lbs fixed v2.unv

#	Symbol	Definition	Section	Freq. (Hz)	Damping (%)	Gen. Mass (kgm ²)	Config	PRC (%)
001	AQ1	1st rotation	ailerons (fixed)	9,67	2,42	43,56	90,06	100
002	S1	1st bending	wings	10,10	1,30	23,28	1,01	99
003	SQ1	1st rotation	ailerons (fixed)	14,41	1,74	13,36	90,10	92
004	AHZ1	1st swing	horizontal fin	15,26	1,79	64,40	4,02	97
005	SHR1	1st rotation	elevator (fixed)	17,81	3,73	2,17	10,06	100
006	AS1	1st rotation	rudder (fixed)	20,06	1,34	21,70	11,11	97
007	AZ1	1st swing	wings and body	22,08	2,05	25,56	4,09	98
008	AHR1	1st torsion	elevator	26,10	2,40	4,95	10,12	96
009	A1	1st bending	wings	28,22	1,92	37,01	2,06	96
010	ATS1	1st torsion	rudder	29,32	2,21	21,75	11,08	95
011	SQT1	1st torsion	ailerons	29,78	2,29	4,58	92,10	96
012	AQT1	1st torsion	ailerons	29,97	1,05	11,74	92,22	96
013	SZ1	1st swing	wings	31,40	2,48	62,86	4,13	86
014	AH1	1st bending	horizontal fin	45,09	1,28	59,54	2,13	92
015	AS2	2nd rotation	rudder (fixed)	45,43	0,69	2,78	11,28	99
016	SHRT1	1st torsion	elevator	57,28	0,52	33,63	13,27	96
017	AT1	1st torsion	wings	58,75	1,94	47,18	1,31	93
018	SH1	1st bending	horizontal fin	62,76	2,05	5,85	6,12	89
019	ST1	1st torsion	wings	64,28	1,49	28,19	1,27	94
020	SHRT2	2nd torsion	elevator	67,26	2,43	4,85	10,18	93
021	S2	2nd bending	wings	80,76	0,90	56,70	1,42	88
Ave.:								95

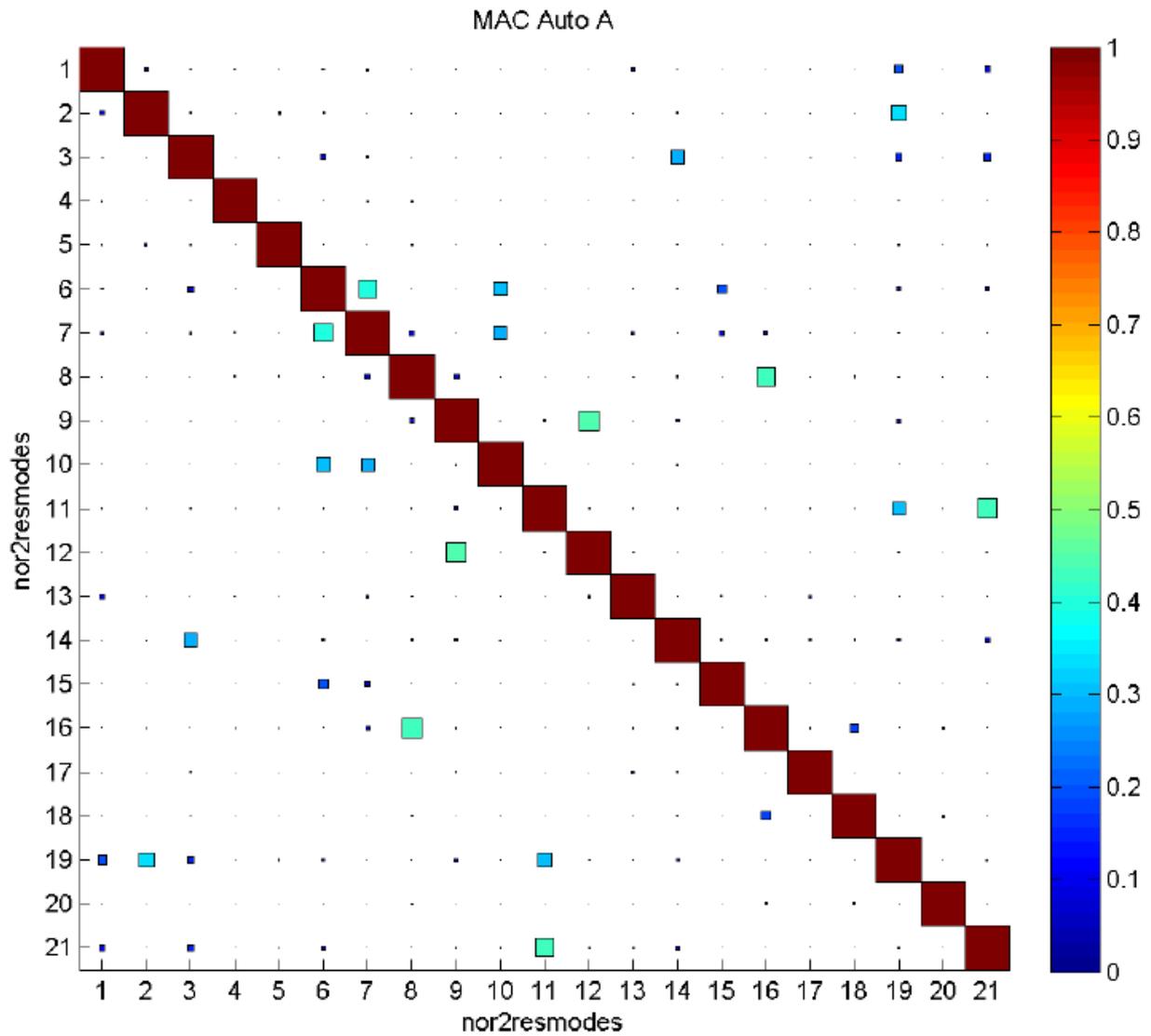


Figure 5: Modal assurance criterion matrix (MAC) for the Eigen vectors evaluated from the time series of the ground vibration test for the CH601XL with minimum take off weight and fixed controls, control cables adjusted to 5 lbs.

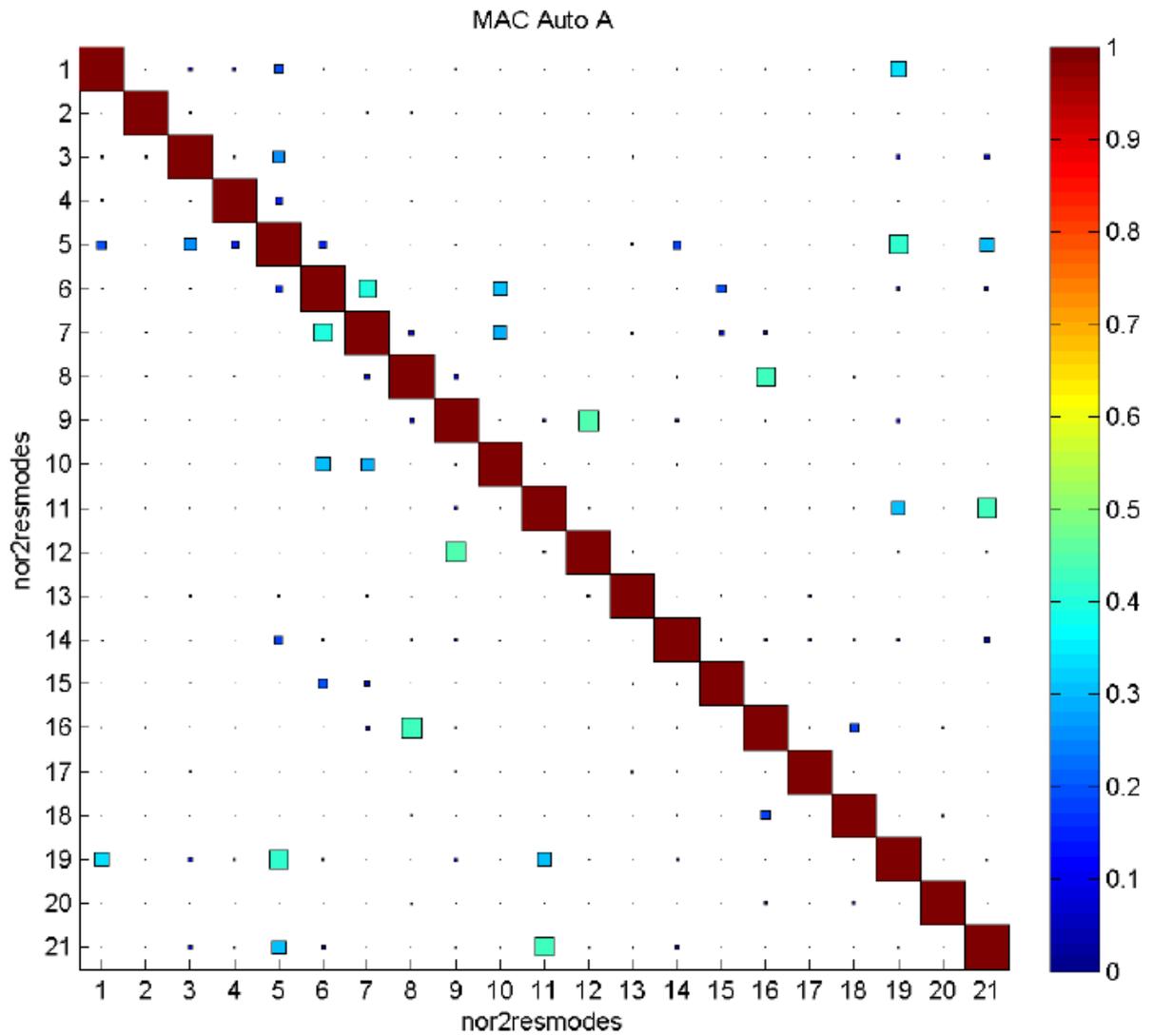


Figure 6: Modal assurance criterion matrix for the Eigen vectors evaluated from the time series of the ground vibration test for the CH601XL with minimum take off weight and fixed controls, control cables adjusted to 30 lbs.

Table 3: Modal data from GVT for CH601XL with minimum take off weight and fixed controls, control cables adjusted to 45 lbs.

Datafile: CH601XL basic 45lbs fixed v2.unv

#	Symbol	Definition	Section	Freq. (Hz)	Damping (%)	Gen. Mass (kgm ²)	Config	PRC (%)
001	S1	1st bending	wings	10,10	1,30	23,28	1,01	99
002	AHZ1	1st swing	horizontal fin	15,26	1,79	64,40	4,02	97
003	AQ1	1st rotation	ailerons (fixed)	15,63	2,15	26,10	92,06	91
004	SHR1	1st rotation	elevator (fixed)	17,81	3,73	2,17	10,06	100
005	SQ1	1st rotation	ailerons (fixed)	18,42	3,27	3,83	92,09	90
006	AS1	1st rotation	rudder (fixed)	20,06	1,34	21,70	11,11	97
007	AZ1	1st swing	wings and body	22,08	2,05	25,56	4,09	98
008	AHR1	1st torsion	elevator	26,10	2,40	4,95	10,12	96
009	A1	1st bending	wings	28,22	1,92	37,01	2,06	96
010	ATS1	1st torsion	rudder	29,32	2,21	21,75	11,08	95
011	SQT1	1st torsion	ailerons	29,78	2,29	4,58	92,10	96
012	AQT1	1st torsion	ailerons	29,97	1,05	11,74	92,22	96
013	SZ1	1st swing	wings	31,40	2,48	62,86	4,13	86
014	AH1	1st bending	horizontal fin	45,09	1,28	59,54	2,13	92
015	AS2	2nd rotation	rudder (fixed)	45,43	0,69	2,78	11,28	99
016	SHRT1	1st torsion	elevator	57,28	0,52	33,63	13,27	96
017	AT1	1st torsion	wings	58,75	1,94	47,18	1,31	93
018	SH1	1st bending	horizontal fin	62,76	2,05	5,85	6,12	89
019	ST1	1st torsion	wings	64,28	1,49	28,19	1,27	94
020	SHRT2	2nd torsion	elevator	67,26	2,43	4,85	10,18	93
021	S2	2nd bending	wings	80,76	0,90	56,70	1,42	88
Ave:								94

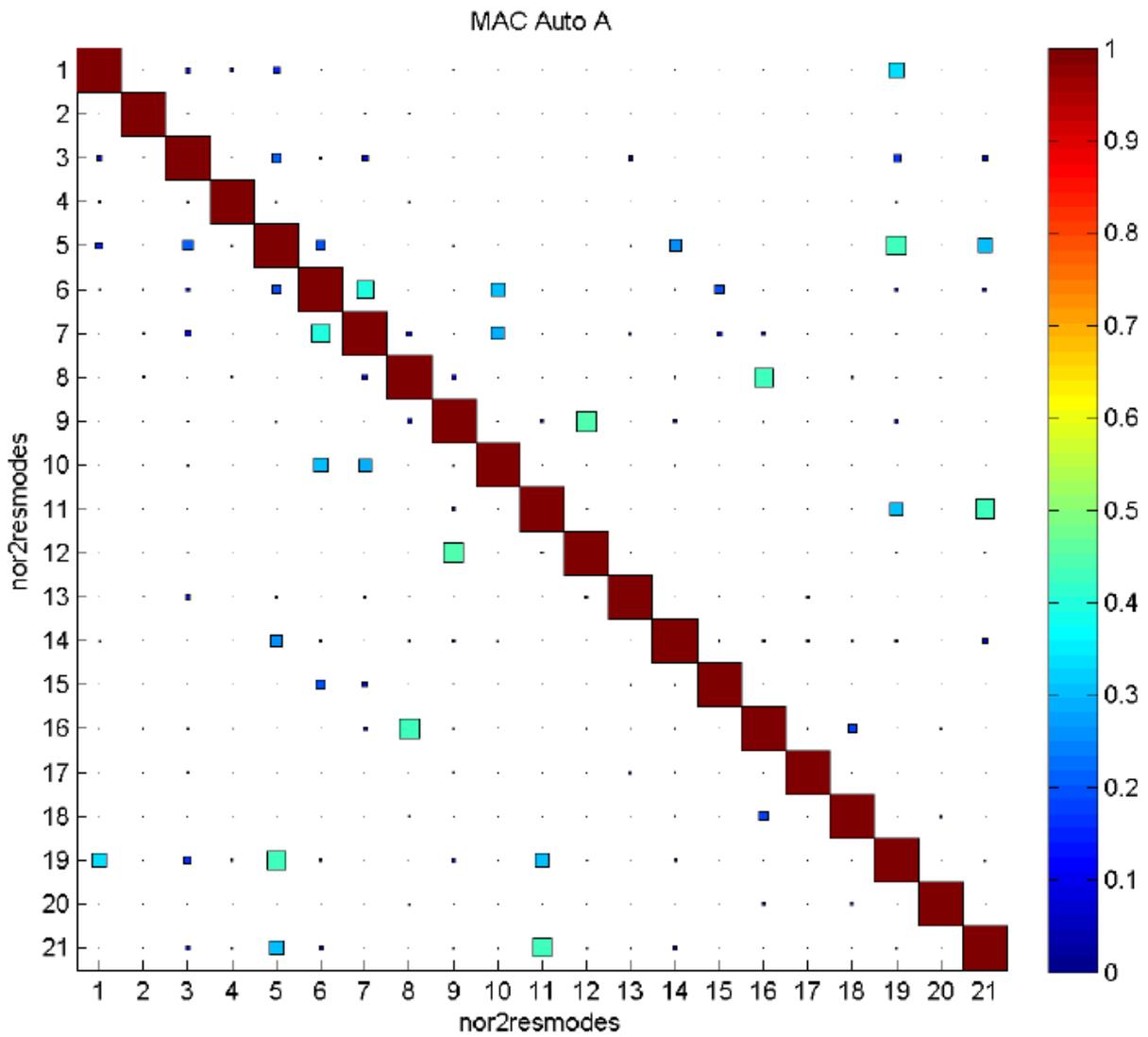


Figure 7: Modal assurance criterion matrix for the Eigen vectors evaluated from the time series of the ground vibration test for the CH601XL with minimum take off weight and fixed controls, control cables adjusted to 45 lbs.

Modal data from GVT for CH601XL with minimum take off mass and free controls

After evaluating the measurements of the ground vibration test for the CH601XL with minimum take off mass and free controls the values for the Eigen frequencies, the generalized masses and modal damping are obtained. The value PRC (Phase Resonance Criterion) is one of the two quality indicators used in this report. If the value PRC is better than 95% the excitation of the corresponding Eigen mode was successful. For PRC values smaller the 80% another measurement with shaker positions in the antinodes of an actual mode is advised.

In order to work out robust flutter margins with respect to the possible variances of control cable tension of the airplane in service, a total of four modal measurements are performed for the CH601XL. Nevertheless if the controls are left free the modal values remain unchanged.

Table 4: Modal data from GVT for CH601XL with minimum take off weight and free controls

Datafile: CH601XL basic 30lbs free v2.unv

#	Symbol	Definition	Section	Freq. (Hz)	Damping (%)	Gen. Mass (kgm ²)	Config	PRC (%)
003	QR1	1st rotation	ailerons (free)	15,59	3,25	4,51	14,05	98
004	QS1	1st rotation	ailerons (free)	17,46	3,59	2,53	14,06	96
005	HR1	1st rotation	elevator (free)	18,51	1,77	18,01	13,06	94
006	ASR1	1st rotation	rudder (free)	20,24	1,11	49,22	12,19	98
007	AZ1	1st swing	wings and body	22,08	2,05	25,56	4,09	98
008	AHR1	1st torsion	elevator	26,10	2,40	4,95	10,12	96
009	A1	1st bending	wings	28,22	1,92	37,01	2,06	96
010	ATS1	1st torsion	rudder	29,32	2,21	21,75	11,08	95
011	SQT1	1st torsion	ailerons	29,78	2,29	4,58	92,10	96
012	AQT1	1st torsion	ailerons	29,97	1,05	11,74	92,22	96
013	SZ1	1st swing	wings	31,40	2,48	62,86	4,13	86
014	HR2	2nd rotation	elevator (free)	42,81	2,12	16,64	13,11	99
015	AH1	1st bending	horizontal fin	45,09	1,28	59,54	2,13	92
016	SHRT1	1st torsion	elevator	57,28	0,52	33,63	13,27	96
017	AT1	1st torsion	wings	58,75	1,94	47,18	1,31	93
018	SH1	1st bending	horizontal fin	62,76	2,05	5,85	6,12	89
019	ST1	1st torsion	wings	64,28	1,49	28,19	1,27	94
020	SHRT2	2nd torsion	elevator	67,26	2,43	4,85	10,18	93
021	S2	2nd bending	wings	80,76	0,90	56,70	1,42	88
Ave.								95

A second indication for the quality of the modal data is the Modal assurance criterion matrix (MAC) which shows the result of the orthogonality test of the Eigen modes found with the ground vibration test (see Figure 8).

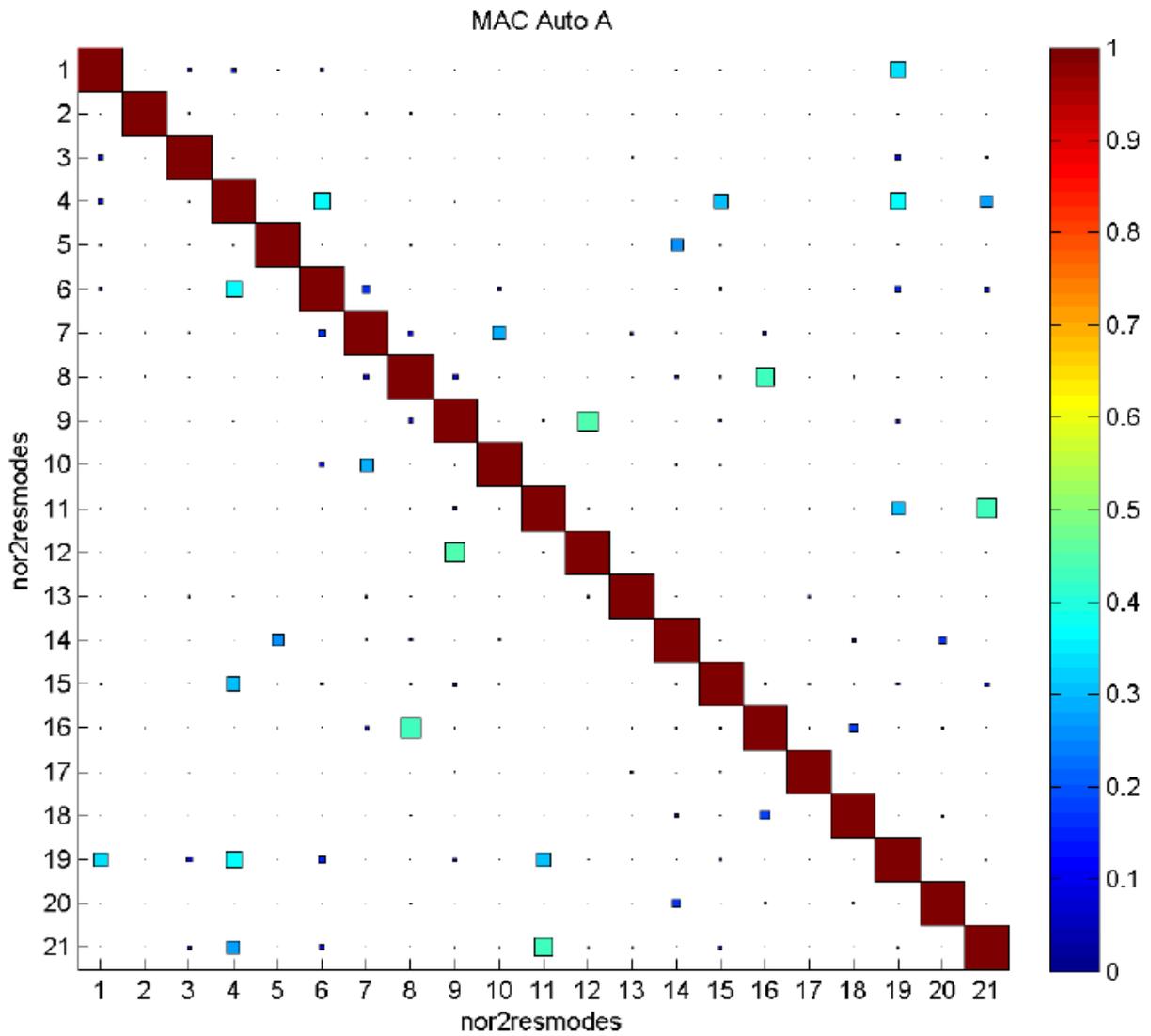


Figure 8: Modal assurance criterion matrix for the Eigen vectors evaluated from the time series of the GVT for the CH601XL with minimum take off mass and free controls.

3. Flutter calculation CH601XL

To calculate the critical flight speed, which indicates the beginning of a possible flutter phenomenon the aeroelastic model of CH601XL must be established. The entire surface of the airplane is discretized with Doublet Lattice Elements (DLE) with the corresponding module of the software package ZAERO⁵. Figure 10 shows the results of this modeling.

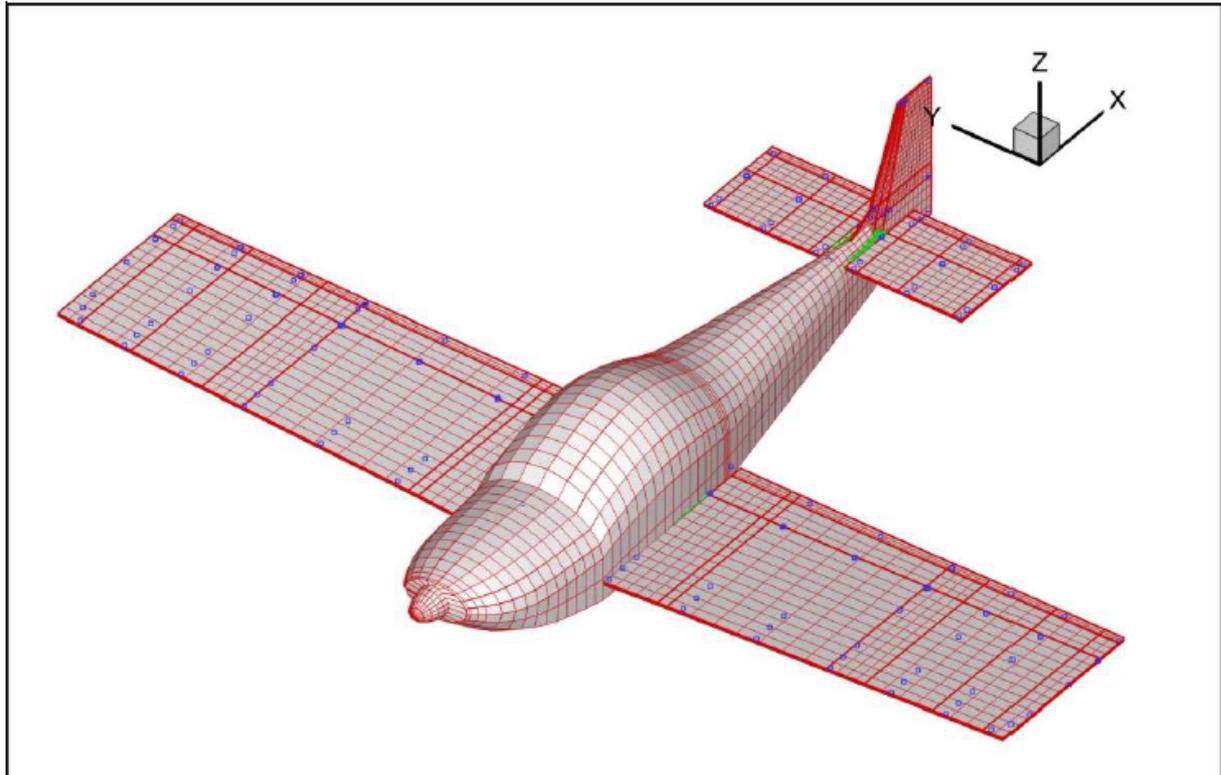


Figure 9: Aeroelastic Model of the CH601XL

After modeling the skin of the airplane the natural vibration modes identified in the time series evaluation from the ground vibration test are imported into the ZAERO program. Each vibration mode is connected to the DLE elements of the aircrafts surface by three dimensional splining methods. The result of this procedure is exported from ZAERO for each mode using standard data sets to allow the printing or animation of these modes. In this work the IDEAS standard universal file format is used. The animation and the images of the modes are produced with the MATLAB toolbox SDTools⁶. The structural dynamic toolbox SDTools allows both, FEA calculations and time series analysis. The first three splined natural modes out of 18 for the CH601XL with controls fixed and cable tension adjusted to the nominal value are shown in Figures 11 through 13. The first three splined natural modes out of 18 for the CH601XL with controls fixed and cable tension adjusted to a value as low as 5 lbs are shown in Figures 14 through 16. The rest of the natural modes for nominal control cable tension as well as for low cable tensions (5 lbs and 15 lbs) and higher cable tension (45 lbs) can be found on the project- DVD as JPG- files and UNV- Files together with the corresponding MATLAB animation source codes.

⁵ ZAERO, Users manual, Version 8.2, March 2008, www.zonatech.com, downloadable PDF

⁶ SDTools, Users manual, Version 6.0, 2008, www.sdtools.com, downloadable PDF

CH601XL Min Mass, Controls fixed, 30lbs, Mode No. 1, 10.099 Hz

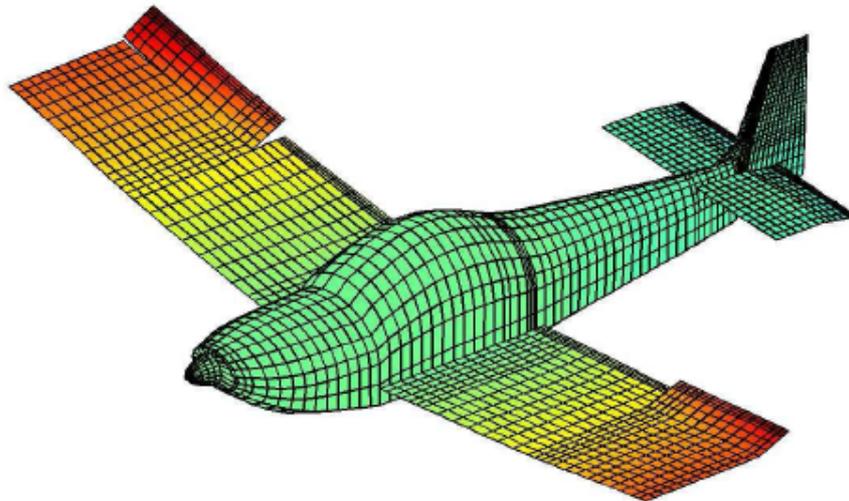


Figure 10: First natural mode of the CH601XL with minimum take off weight, controls fixed and cable tension adjusted to the nominal value 30lbs

CH601XL Min Mass, Controls fixed, 30lbs, Mode No. 2, 15.264 Hz

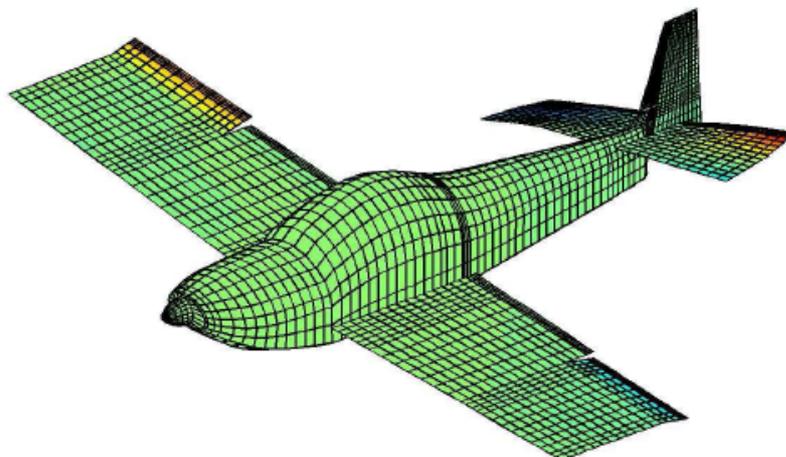


Figure 11: Second natural mode of the CH601XL with minimum take off weight, controls fixed and cable tension adjusted to the nominal value 30lbs



CH601XL Min Mass, Controls fixed, 30lbs, Mode No. 3, 15.377 Hz

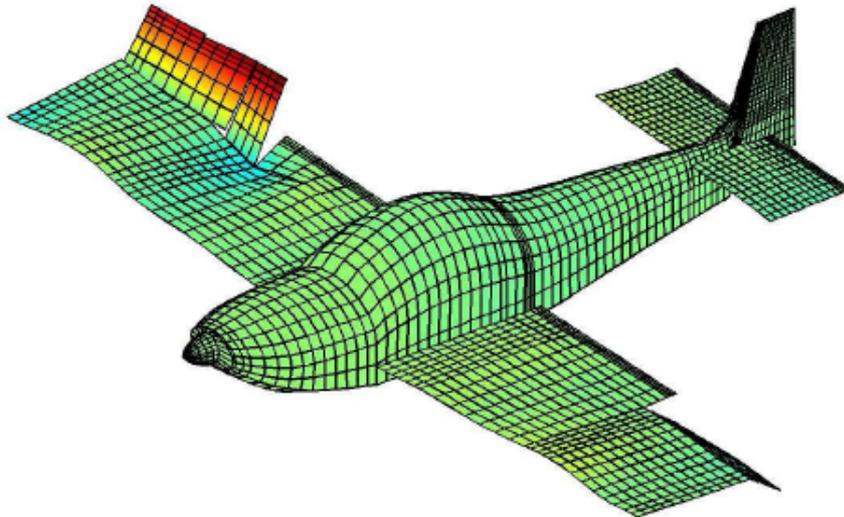


Figure 12: Third natural mode of the CH601XL with minimum take off weight, controls fixed and cable tension adjusted to the nominal value 30lbs

CH601XL Min Mass, Controls fixed, 5lbs, Mode No. 1, 9.665 Hz

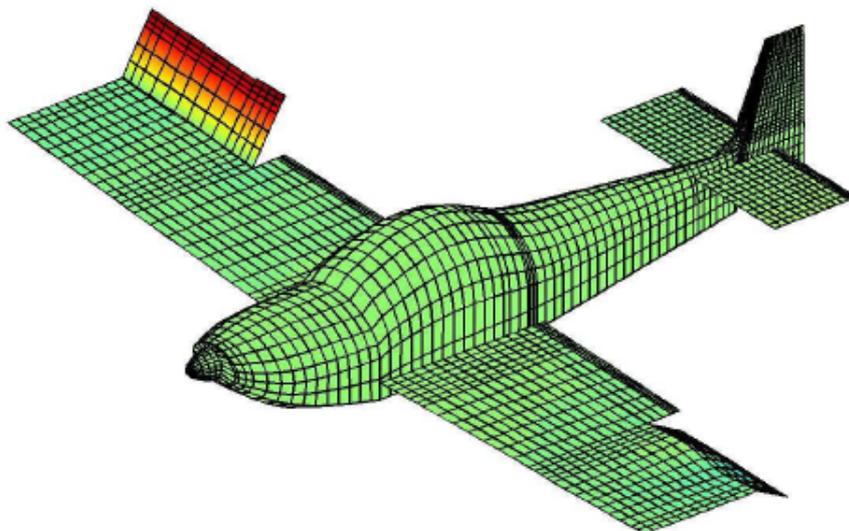


Figure 13: First natural mode of the CH601XL with minimum take off weight, controls fixed and cable tension adjusted to 5lbs

CH601XL Min Mass, Controls fixed, 5lbs, Mode No. 2, 10.099 Hz

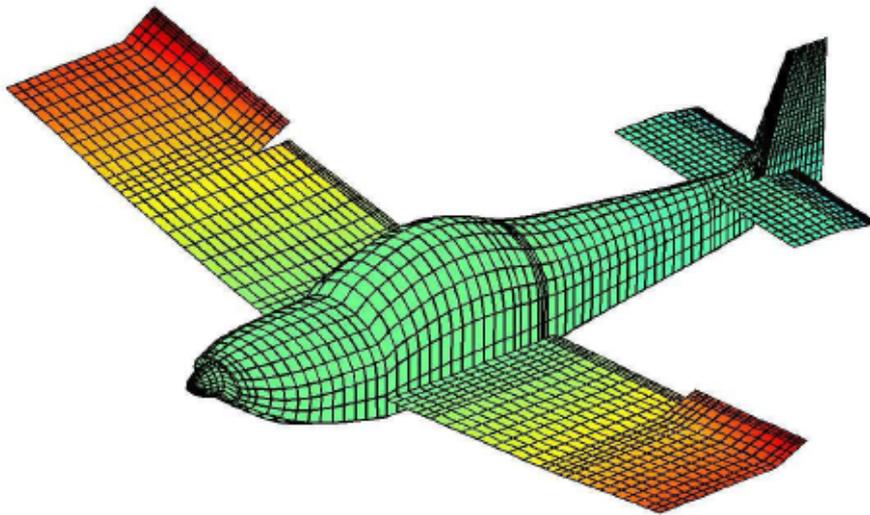


Figure 14: Second natural mode of the CH601XL with minimum take off weight, controls fixed and cable tension adjusted to 5lbs

CH601XL Min Mass, Controls fixed, 5lbs, Mode No. 3, 14.411 Hz

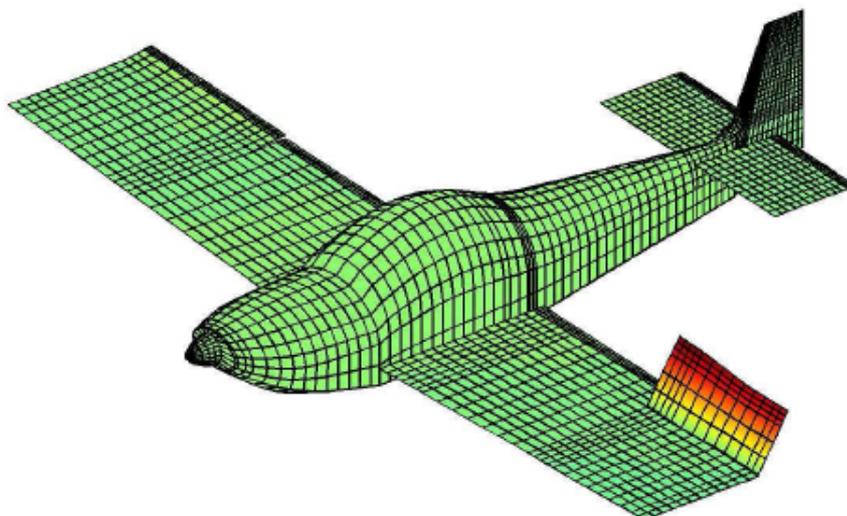


Figure 15: Third natural mode of the CH601XL with minimum take off weight, controls fixed and cable tension adjusted to 5lbs

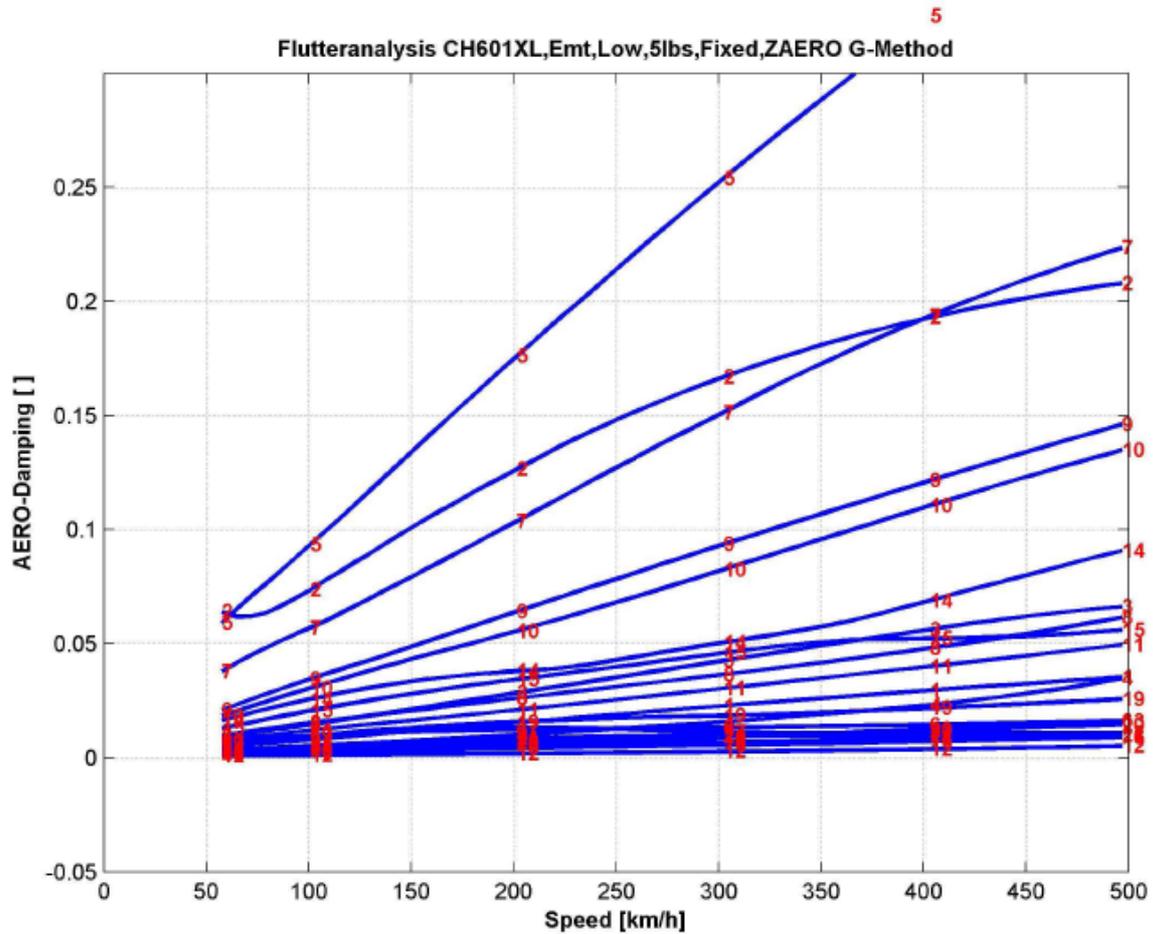


Figure 17: Aerodynamic damping for the CH601XL with minimum take off mass and blocked controls (aileron, elevator and rudder) at low altitude flight from 60 km/h up to 500 km/h. Control cable tension adjusted to a very low value (15 lbs).

As shown in Figure 18 and Figure 19 the airspeed dependent Eigen frequencies of the aileron modes (Mode 2 and Mode 3 in Figure 18, Mode 1 and Mode 3 in Figure 19)⁷ are reduced significantly only at low air speed. At higher airspeed the aileron control in both cases appears to become stiffer. This is the usual experience of a pilot in flight.

⁷ The frequencies in ZAERO are sorted with respect to their values in ascending order

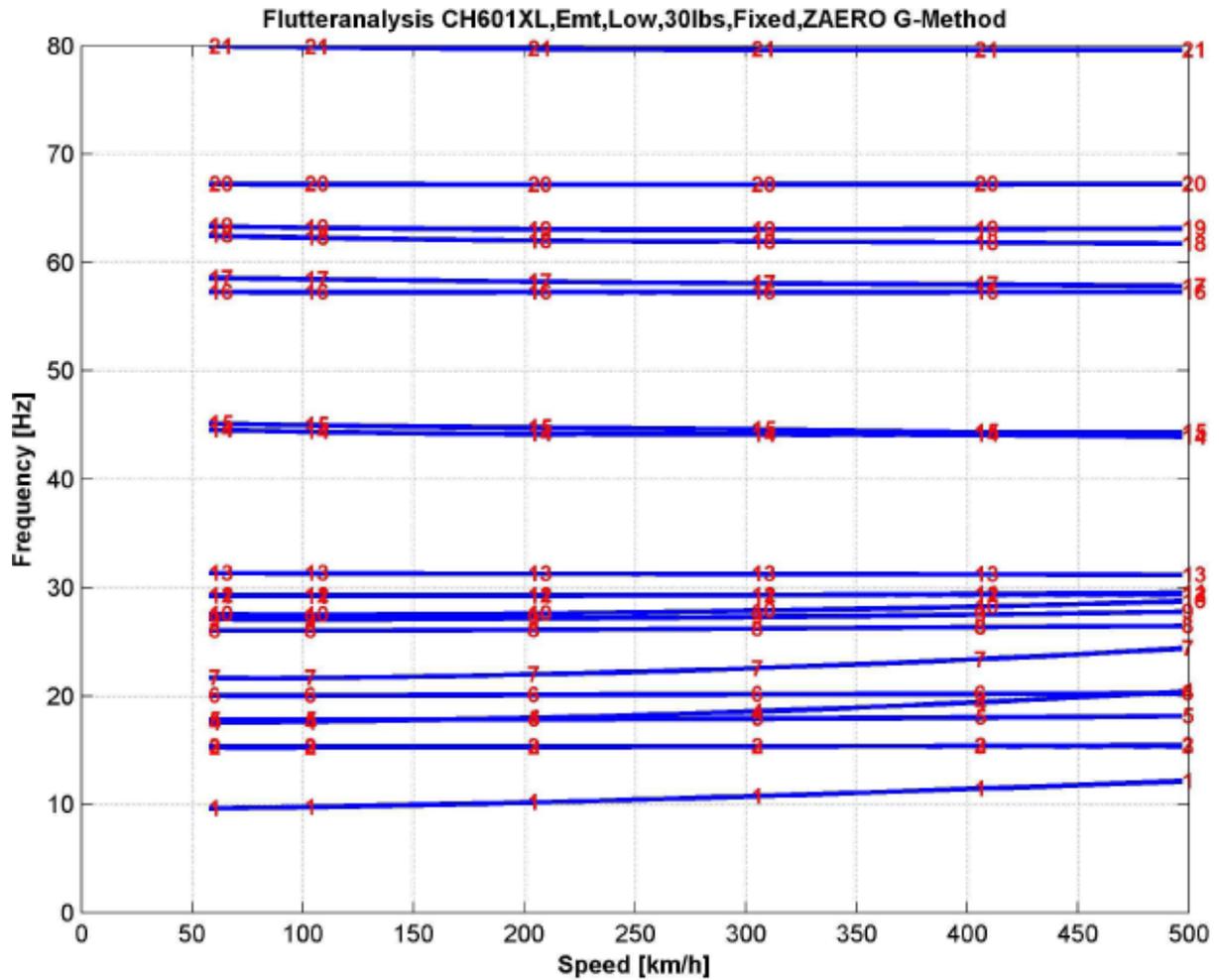


Figure 18: Eigen Frequencies for the CH601XL with minimum take off mass and blocked controls (aileron, elevator and rudder) at low altitude flight from 60 km/h up to 500 km/h. Control cable tension adjusted to nominal value (30 lbs).

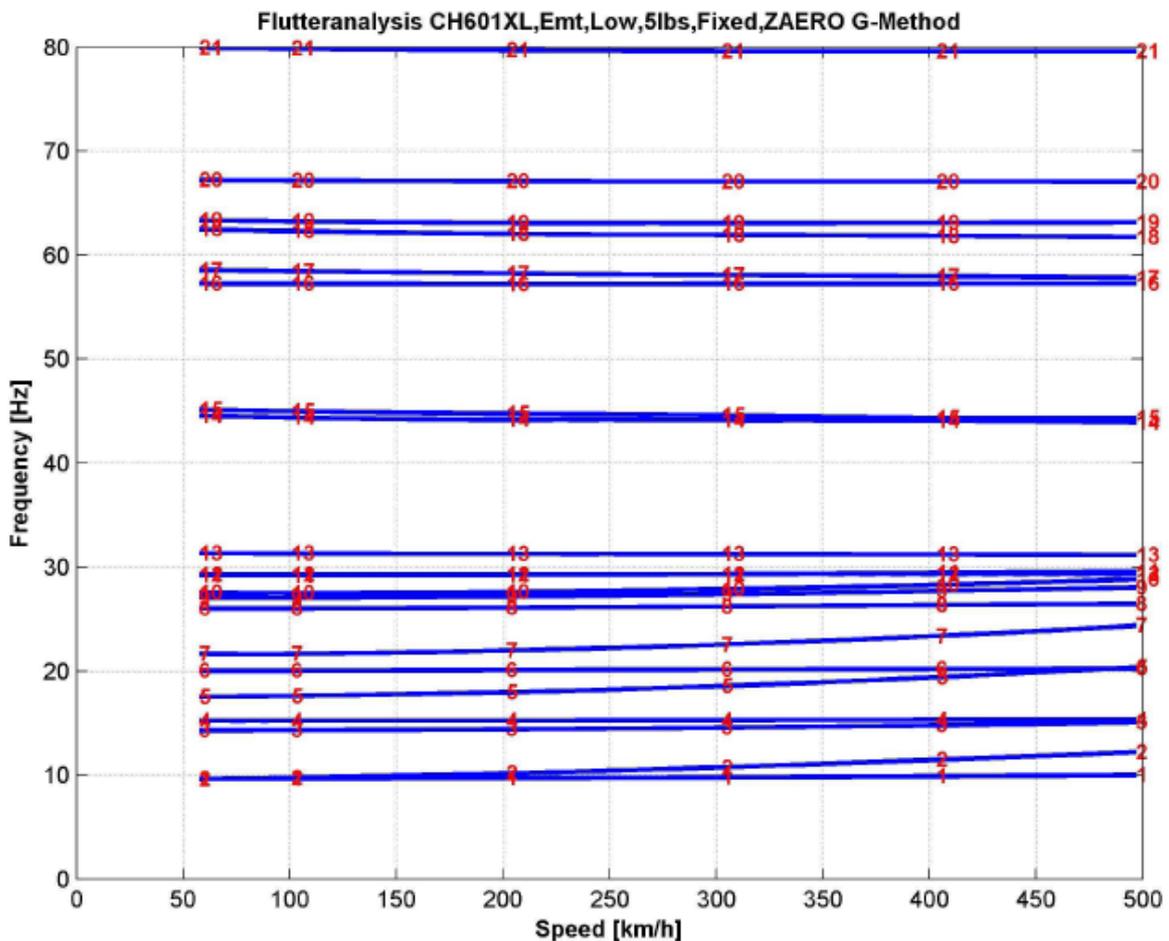


Figure 19: Eigen Frequencies for the CH601XL with minimum take off mass and blocked controls (aileron, elevator and rudder) at low altitude flight from 60 km/h up to 500 km/h. Control cable tension adjusted to a very low value (5 lbs).

4. Flutter results for the CH601XL

Flutter calculations have been performed for the CH601XL based on the results of complete ground vibration tests up to Eigen frequencies of 80 Hz. All results, the input and output files for the software package ZAERO, as well as all pre- and post processing MATLAB program codes are stored on the corresponding project DVD CH601XL. The files on the DVD CH601XL allow complete analysis and reproduction all computed results:

- minimum and maximum take off mass
- controls fixed and free
- cable tensions of aileron control system from 5 lbs to 45 lbs
- low altitude flight (MSL) and high altitude flight (5000 m)

No tendency to flutter or divergence was found within the flight envelope. The analysis does not show any reason to install mass balancing weights nor the need for spades.

5. Summary

JAR-23 guidelines require testing to ensure that “the airplane is free from flutter, control reversal and divergence for any condition of operation within the limit $V\sim n$ envelope”. With the classical linear approach for flutter analysis with ground vibration test and up to date flutter calculations using the software package ZAERO, no aeroelastic instability was found within the flight envelope of the CH601XL.

When the flap stops are installed according to the manufacturer's specifications is mounted and the cable tensions are within the specified tolerances set by the manufacturer, the occurrence of flutter with the CH601XL is improbable within the well defined flight envelope.

The analysis in this report is based on linear methodology. The analysis of possible nonlinear vibrations due to structural instabilities was not the subject of this investigation.

6. Assumptions and Final Remarks

In order to insure that the flutter results worked out in this report will be valid, the authors assume that the following conditions will be in place:

1. All control cable tensions will be set and maintained as per manufacturer's specifications.



Figure 20: Adjusting control cable tension (see XLphotoguide.pdf)

2. The flap gap stops for the retracted landing flaps (see Figure 21) must be installed



Figure 21: Flap gap stop, Part No. 6S3-1

3. Aircraft must be operated within specified speed limitations as set out by the manufacturer. This includes VF, VA, VC and VNE (see Flight Manual or plans for details).

TECHNICAL DATA

Wing Area: 134 sq. ft (12.5 sq. m.)
 Wing Airfoil (profile): Riblet Wing GA 35-A-415
 Wing Span: 27' (8.23m)
 Wing Chord root 5'-3" (1.6m)
 tip 4'-8" (1.42m)
 Wing Aspect Ratio: 5.4
 H.Tail and V. Tail: NACA 0012
 Horizontal Tail Span: 7'-7" (2.3m)
 Length: 20' (6.1m)
 Rudder Tip Height: 6'-6" (1.98m)

Suitable Power Range: 80 to 125 BHP
 Design Load Factor (Ultimate): +/- 6 G @ 1320 lbs.
 Gross Weight: 1080 lbs (490 kg)

DESIGN SPEED LIMITATIONS (CALIBRATED AIRSPEED)

V _A	MANEUVERING SPEED	103 MPH (166 Km/h)
V _C	DESIGN CRUISE SPEED	124 MPH (200 Km/h)
V _{FE}	MAX FLAP EXTENDED	80 MPH (130 Km/h)
V _{NE}	NEVER-EXCEED SPEED	160 MPH (260 Km/h)
V _{S1}	STALL SPEED (no flaps)	51 MPH (80 Km/h)
V _{S0}	FLAPS EXTENDED STALL	41 MPH (65 Km/h)

AIRSPEED MARKINGS

RED LINE = V_{NE}
 YELLOW ARC = V_C to V_{NE}
 GREEN ARC = V_{S1} to V_C
 WHITE ARC = V_{S0} to V_{FE}

SERIAL NO: 6-	ZODIAC CH 601 XL ULM	THREE VIEWS GENERAL SPECIFICATIONS	6-UL-01
		copyright © 2003 CHRIS HEINTZ zenithair.com DATE: 03/2008	

Figure 22: Speed limits (extract from front page of CH601XL plans)

4. Aileron deflections measured at the hinge axis must all be kept within the specified values. Control stop(s) must be installed as per manufacturer specifications to ensure deflections remain within acceptable ranges (see Figure 23 for example).

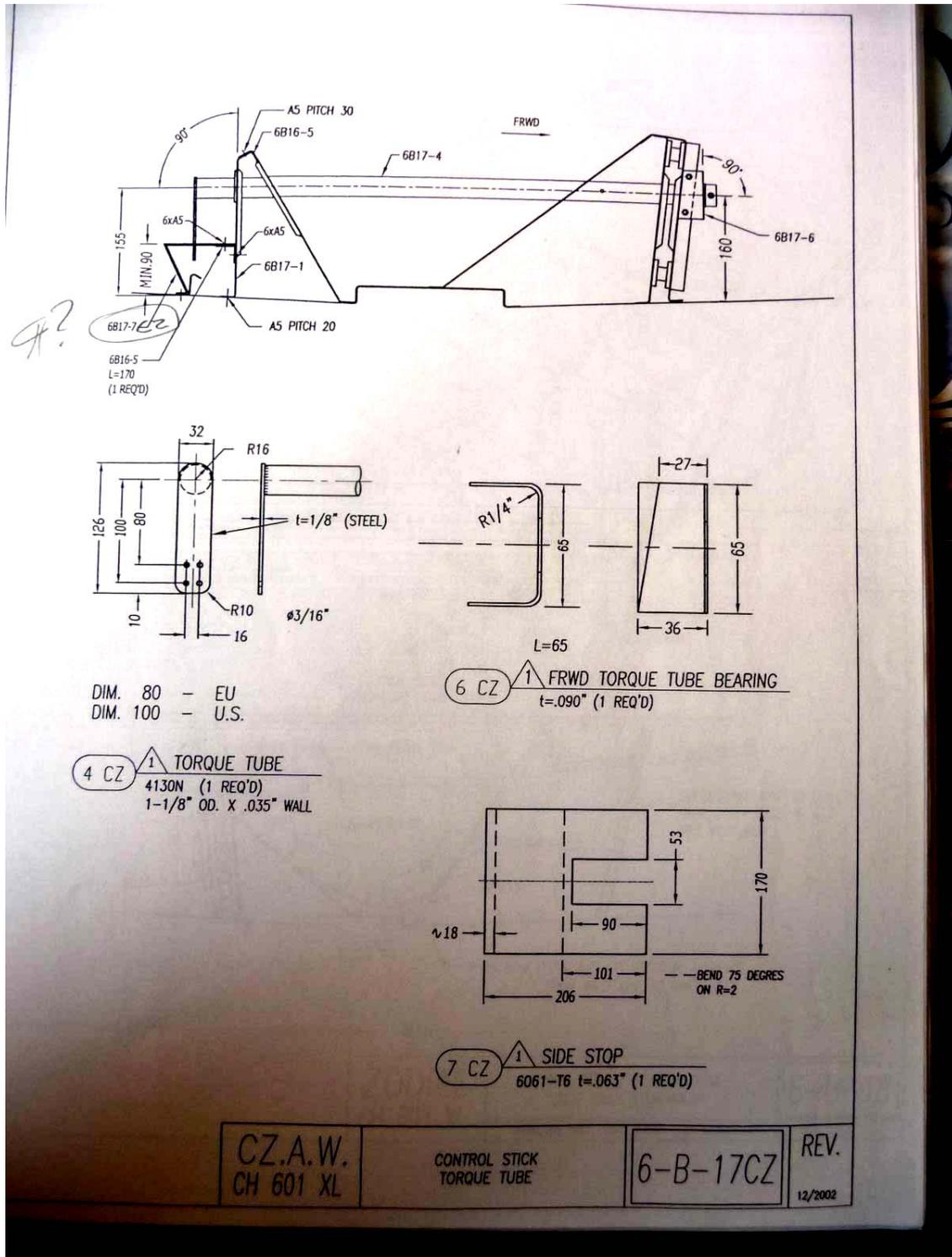


Figure 23: One acceptable aileron-stop design (as per LTF-UL certified CH 601 XL)

7. Remarks and recommendations on Aileron Mass Balancing and Spades

A number of individual Zodiac owners as well as government agencies have recommended the installation of traditional aileron mass balancing as a means to mitigate any risk of flutter with the Zodiac design. Based on the standard airframe design examined and on the GVT results and linear approach of the flutter analysis documented in this report, mass balancing for the ailerons of the CH601XL (see example Figure 24) or the use of spades (see Figure 25) is not needed or justified.

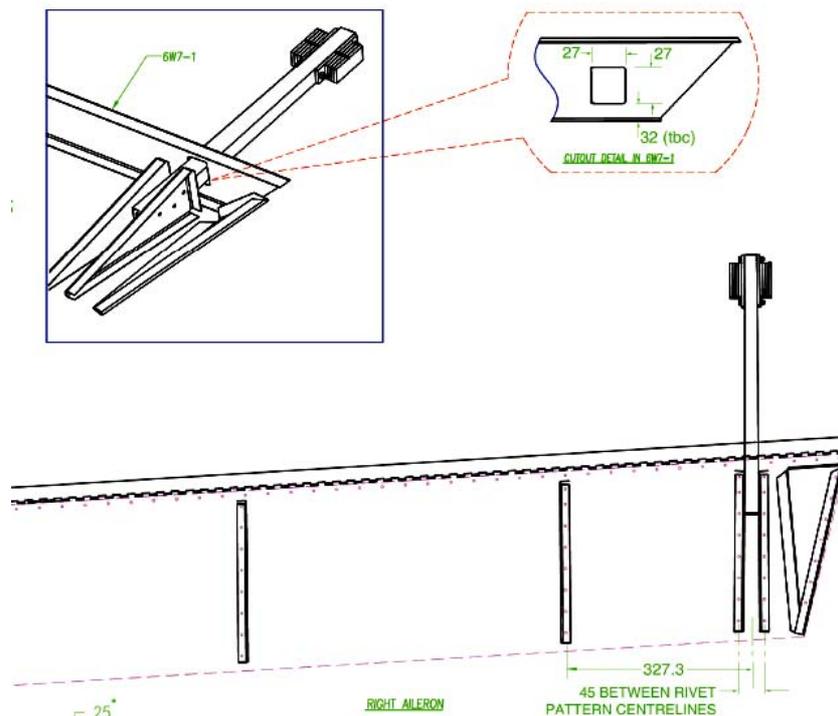


Figure 24: Proposal for mass balancing



Figure 25: Proposal for spades

While mass balancing of the ailerons is generally believed to prevent flutter, the extra weight associated with control-surface mass balancing could have negative consequences if not properly designed and/or supported. It is possible that modifications to the standard control system and/or basic airframe structure of the Zodiac could be necessary to properly install aileron mass balancing on the CH650E.

As any new modification (such as mass balancing) can potentially be associated with new “randomly excited non-linear vibrations”, it must therefore be “sound” (sensible) through logic and reasoning and effective as demonstrated through testing. Sometimes, if one does not know exactly what one is doing, one can make matters worse with a well-intentioned modification to an aircraft.

Hamburg, June 6, 2009



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